

$$U_{an} := 230V \quad I_{an} := 26.1A \quad P_n := 5kW \quad \omega_n := 150 \cdot \frac{\text{rad}}{\text{s}}$$

$$R_a := 1.1\Omega \quad L_a := 10\text{mH} \quad J_m := 0.06\text{kg}\cdot\text{m}^2 \quad T_a := \frac{L_a}{R_a} = 9.091\cdot\text{ms}$$

$$D := 0.1\text{m} \quad J_b := 0.1\text{kg}\cdot\text{m}^2 \quad c := 60 \frac{\text{N}\cdot\text{m}}{\text{rad}}$$

Usvojimo bazne vrednosti:

$$U_b := U_{an} \quad I_b := I_{an} \quad \omega_b := \omega_n \quad \Delta\theta_b := 1\text{rad} \quad \text{Osnovne bazne veličine}$$

$$R_b := \frac{U_b}{I_b} \quad M_b := \frac{U_b \cdot I_b}{\omega_b} \quad \psi_{fb} := \frac{U_b}{\omega_b} \quad \text{Izvedene bazne veličine}$$

Normalizacija

$$R_{a-} := \frac{R_a}{R_b} \quad \psi_{fn} := \frac{U_{an} - R_a \cdot I_{an}}{\omega_n} = 1.342 \text{ Wb} \quad \psi_{fn-} := \frac{\psi_{fn}}{\psi_{fb}} \quad \text{ili} \quad 1 - R_{a-} = 0.875$$

$$T_{m1} := \frac{J_m \cdot \omega_b}{M_b} \cdot \frac{1}{s} \quad T_{m2}(M_t) := \left(J_b + \frac{M_t \cdot D^2}{4} \right) \cdot \frac{\omega_b}{M_b} \cdot \frac{1}{s} \quad c_- := c \cdot \frac{\Delta\theta_b}{M_b} = 1.499$$

$$T_{m1} = 0.225 \quad T_{a-} := T_a \cdot \frac{1}{s} \quad g = 9.807 \frac{\text{m}}{\text{s}^2}$$

Matrica sistema

Matrica ulaza

$$A_-(M_t) := \begin{pmatrix} -\frac{1}{T_a} & -\frac{\psi_{fn-}}{R_{a-} \cdot T_a} & 0 & 0 \\ \frac{\psi_{fn-}}{T_{m1}} & 0 & 0 & -\frac{c_-}{T_{m1}} \\ 0 & 0 & 0 & \frac{c_-}{T_{m2}(M_t)} \\ 0 & 1 & -1 & 0 \end{pmatrix}$$

$$B(M_t) := \begin{pmatrix} \frac{1}{R_{a-} \cdot T_a} & 0 \\ 0 & 0 \\ 0 & -\frac{1}{T_{m2}(M_t)} \\ 0 & 0 \end{pmatrix}$$

B) Stacionarno stanje

$$u_{aB} := 0.5 \quad i_{aB} := \frac{20A}{I_b} = 0.766$$

Sistem jednačina koje treba rešiti

$$U_a - \omega_1 \cdot \psi_{fn} - R_a \cdot I_a = 0$$

$$\psi_{fn} \cdot I_a - c \cdot \Delta\theta = 0$$

$$\omega_1 = \omega_2 \quad m_m = c \cdot \Delta\theta$$

$$\omega_{1B} := \frac{u_{aB} - R_{a_} \cdot i_{aB}}{\psi_{fn_}} = 0.462 \quad \Delta\theta_B := \frac{\psi_{fn_} \cdot i_{aB}}{c_} = 0.447 \quad m_m := c_ \cdot \Delta\theta_B = 0.671$$

$$M_{tB} := m_m \cdot M_b \cdot \frac{2}{g \cdot D} = 54.736 \text{ kg}$$

C) promena smeru - spuštanje tereta

$$u_{aC} := -0.5 \quad \text{Promena polariteta napona indukta}$$

$$i_{aC} := \frac{m_m}{\psi_{fn_}} = 0.766 \quad \omega_{1C} := \frac{u_{aC} - R_{a_} \cdot i_{aC}}{\psi_{fn_}} = -0.681 \quad \Delta\theta_C := \frac{\psi_{fn_} \cdot i_{aC}}{c_} = 0.447$$

$$u_{aC2} := 0.5 \quad \psi_{fnC} := -\psi_{fn_} \quad \text{Promena polariteta napona pobude}$$

tj. promena smeru pobude.

$$i_{aC2} := \frac{m_m}{\psi_{fnC}} = -0.766 \quad \omega_{1C2} := \frac{u_{aC2} - R_{a_} \cdot i_{aC2}}{\psi_{fnC}} = -0.681 \quad \Delta\theta_{C2} := \frac{\psi_{fnC} \cdot i_{aC2}}{c_} = 0.447$$

D) vrednosti matrica

$$T_{m2}(M_{tB}) \cdot s = 0.888 \text{ s}$$

$$A_{-}(M_{tB}) = \begin{pmatrix} -110 & -771.226 & 0 & 0 \\ 3.892 & 0 & 0 & -6.667 \\ 0 & 0 & 0 & 1.689 \\ 0 & 1 & -1 & 0 \end{pmatrix} \quad B(M_{tB}) = \begin{pmatrix} 881.226 & 0 \\ 0 & 0 \\ 0 & -1.127 \\ 0 & 0 \end{pmatrix}$$

$$\text{eigenvals}(A_{-}(M_{tB})) = \begin{pmatrix} -60.4 \\ -49.354 \\ -0.123 + 1.298i \\ -0.123 - 1.298i \end{pmatrix}$$