

Opterećenje je nezavisno od brzine i konstantno

$$\omega := 2 \cdot \pi$$

$$m_m := 20 \text{ N} \cdot \text{m}$$

Podaci asinhronog motora

$$U_n := 220 \text{ V} \quad \omega_n := 1440 \cdot \frac{\text{O}}{\text{min}} \quad P := 2$$

$$R_s := 1.54 \Omega \quad R_r := 2.5 \Omega \quad \omega_s := 2 \cdot \pi \cdot 50 \text{ Hz}$$

$$\lambda_s := 0.0088 \text{ H} \quad \lambda_r := \lambda_s$$

$$s_n := \frac{\omega_s - P \cdot \omega_n}{\omega_s} \quad s_n = 4. \% \quad \text{Nominalno klizanje}$$

$$s_p := \frac{R_r}{\sqrt{R_s^2 + \omega_s^2 \cdot (\lambda_s + \lambda_r)^2}} \quad s_p = 43.55659. \% \quad \text{Prevalno klizanje}$$

$$\omega_p := s_p \cdot \frac{\omega_s}{P} \quad \omega_p = 68.419 \cdot \frac{\text{rad}}{\text{s}} \quad \omega_p = 653.349 \cdot \frac{\text{O}}{\text{min}} \quad \text{Meh. prevalna brzina}$$

$$Z(s) := R_s + \frac{R_r}{s} + i \cdot \omega_s \cdot (\lambda_s + \lambda_r) \quad \text{Fazna impedansa}$$

$$I(s) := \frac{U_n}{Z(s)} \quad m_{AC}(s) := 3 \cdot P \cdot \frac{R_r}{s} \cdot \frac{1}{\omega_s} \cdot \frac{U_n^2}{(|Z(s)|)^2}$$

$$I_n := \frac{U_n}{Z(s_n)} \quad I_n = (3.41 - 0.294i) \text{ A} \quad |I_n| = 3.423 \text{ A} \quad \arg(I_n) = -4.935 \cdot \text{deg}$$

$$\cos(\arg(I_n)) = 0.996 \quad \text{Zanemarena struja magnećenja.}$$

Podaci jednosmernog motora

$$U_{an} := 440 \text{ V} \quad I_{an} := 100 \text{ A} \quad \omega_{DCn} := 2500 \cdot \frac{\text{O}}{\text{min}} \quad R_a := 0.17 \Omega$$

$$\Psi_{fn} := \frac{U_{an} - R_a \cdot I_{an}}{\omega_{DCn}} \quad \Psi_{fn} = 1.616 \text{ Wb}$$

a) Koju će brzinu imati pogon ako je uključen samo jednosmerni pogon na nominalni napon, a koju ako je uključen samo asihroni?

$$\omega_{aDC} := \frac{U_{an}}{\Psi_{fn}} - R_a \cdot \frac{m_m}{\Psi_{fn}^2} = 271.019 \cdot \frac{\text{rad}}{\text{s}} \quad \omega_{aDC} = 2.588 \times 10^3 \cdot \frac{\text{O}}{\text{min}}$$

$$s_{\text{poc}} := 0.2 \quad \text{Given} \quad m_{\text{AC}}(s_{\text{poc}}) = m_m \quad s_a := \text{Find}(s_{\text{poc}}) = 0.059$$

$$(1 - s_a) \cdot \frac{\omega_s}{P} = 147.809 \cdot \frac{\text{rad}}{\text{s}} \quad (1 - s_a) \cdot \frac{\omega_s}{P} = 1411.475 \cdot \frac{\text{o}}{\text{min}}$$

b) Pr kojoj brzini će jednosmerni motor razvijati najveći momenat ako su oba motora uključena

$$\omega_b := \frac{\omega_s}{P} (1 + s_p) = 225.498 \cdot \frac{\text{rad}}{\text{s}} \quad \omega_b = 2.153 \times 10^3 \cdot \frac{\text{o}}{\text{min}} \quad s_p = 0.436$$

$$m_{\text{bAC}} := m_{\text{AC}}(-s_p) = -110.053 \cdot \text{N}\cdot\text{m}$$

$$m_{\text{bDC}} := m_m - m_{\text{bAC}} = 130.053 \cdot \text{N}\cdot\text{m}$$

$$u_{\text{bDC}} := \Psi_{\text{fn}} \cdot \omega_b + R_a \cdot \frac{m_{\text{bDC}}}{\Psi_{\text{fn}}} = 378.03 \text{ V} \quad I_{\text{bDC}} := \frac{m_{\text{bDC}}}{\Psi_{\text{fn}}} = 80.491 \text{ A}$$

c) Pri kojoj brzini će jednosmerni motor razvijati najmanji momenat ako su oba motora uključena

$$\omega_c := \frac{\omega_s}{P} (1 - s_p) = 88.661 \cdot \frac{\text{rad}}{\text{s}} \quad \omega_c = 846.651 \cdot \frac{\text{o}}{\text{min}}$$

$$m_{\text{cAC}} := m_{\text{AC}}(s_p) = 63.49 \cdot \text{N}\cdot\text{m} \quad \Psi_{\text{fn}} = 1.616 \text{ Wb}$$

$$m_{\text{cDC}} := m_m - m_{\text{cAC}} = -43.49 \cdot \text{N}\cdot\text{m}$$

$$u_{\text{cDC}} := \Psi_{\text{fn}} \cdot \omega_c + R_a \cdot \frac{m_{\text{cDC}}}{\Psi_{\text{fn}}} = 138.678 \text{ V} \quad I_{\text{cDC}} := \frac{m_{\text{cDC}}}{\Psi_{\text{fn}}} = -26.916 \text{ A}$$

d) Uslov statičke stabilnosti u ovom pogonu kada rade oba motora. Opseg brzina?

$$\left( \frac{d}{d\omega} m_{\text{dc}} \right) + \left( \frac{d}{d\omega} m_{\text{ac}} \right) < \frac{d}{d\omega} m_m \quad \left( \frac{d}{d\omega} m_m \right) = 0$$

e) Kako se može ostvariti brzina jednaka 3/4 sinhronne brzine asinhronog motora, kada su oba motora uključena istovremeno.

$$\omega_a := \frac{3}{4} \cdot \frac{\omega_s}{P} \quad \omega_a = 117.81 \cdot \frac{\text{rad}}{\text{s}} \quad \omega_a = 1125 \cdot \frac{\text{°}}{\text{min}} \quad s_{\text{max}} := \frac{1}{4}$$

$$m_{\text{AC}}(s_a) = 56.452 \cdot \text{N} \cdot \text{m}$$

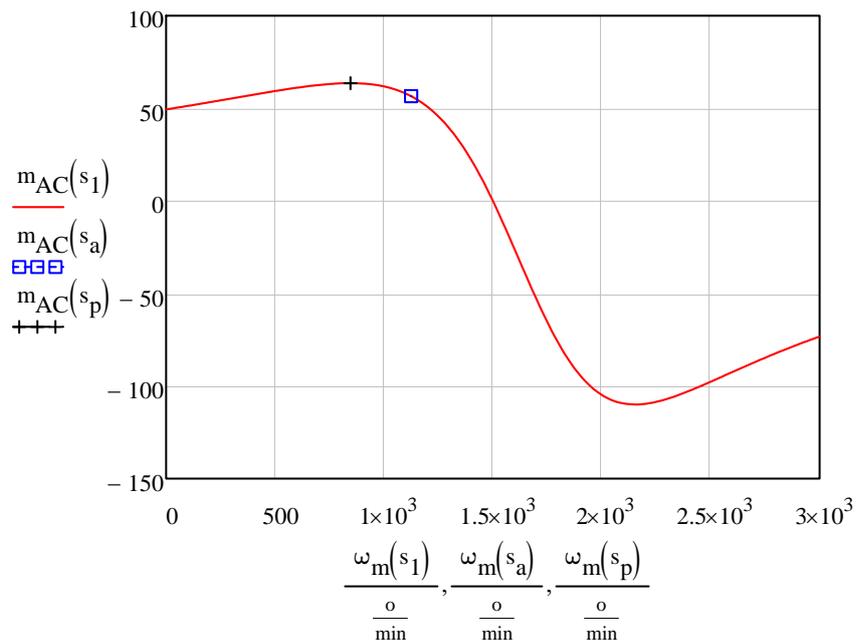
$$m_{\text{DC}} := m_m - m_{\text{AC}}(s_a) \quad m_{\text{DC}} = -36.452 \cdot \text{N} \cdot \text{m}$$

$$I_{\text{DC}} := \frac{m_{\text{DC}}}{\Psi_{\text{fn}}} \quad I_{\text{DC}} = -22.561 \text{ A}$$

$$U_{\text{DC}} := R_a \cdot I_{\text{DC}} + \omega_a \cdot \Psi_{\text{fn}} \quad U_{\text{DC}} = 186.515 \text{ V} \quad \frac{U_{\text{DC}}}{U_n} = 0.848$$

$$\omega_m(s) := \frac{\omega_s}{P} \cdot (1 - s)$$

$$s_1 := 1, 0.99 \dots -1$$



f) Da li je rezim rada asinhronog motora ekonomican?

$$\omega_a = 1125 \cdot \frac{\text{o}}{\text{min}} \qquad \omega_p = 653.349 \cdot \frac{\text{o}}{\text{min}}$$

Posto je tacka sa brzinom vecom od prevalne, zadovoljen je uslov staticke stabilnosti.

Sa druge strane, fazna struja u tom rezimu je veca od nominalne, pa takav rezim ne moze da traje dugo sa stanovista gubitaka i zagrevanja.

$$I(s_a) = (15.505 - 7.429i) \text{ A} \qquad \frac{|I(s_a)|}{|I_n|} = 5.023$$

g) Sta ce se dogoditi ako se u ovom rezimu iskljuci jednosmerni motor, a sta ako se iskljuci asinhroni.

Iskljucenje jednosmernog motora:

$$s_c := 0.1$$

Pocetni pogodak.

Given

$$m_{AC}(s_c) = m_m$$

$$s_c := \text{Find}(s_c) \qquad s_c = 5.902 \cdot \%$$

$$\omega_c := \frac{\omega_s}{p} \cdot (1 - s_c) \qquad \omega_c = 147.809 \cdot \frac{\text{rad}}{\text{s}} \qquad \omega_c = 1411.475 \cdot \frac{\text{o}}{\text{min}}$$

$$I(s_c) = (4.933 - 0.621i) \text{ A}$$

$$|I(s_c)| = 4.972 \text{ A}$$

Iskljucenje asinhronog motora:

$$m_{DC} := m_m$$

$$I_{DC} := \frac{m_{DC}}{\Psi_{fn}} \qquad I_{DC} = 12.378 \text{ A}$$

$$\omega_{DC} := \frac{U_{DC} - R_a \cdot I_{DC}}{\Psi_{fn}} \qquad \omega_{DC} = 114.134 \cdot \frac{\text{rad}}{\text{s}} \qquad \omega_{DC} = 1089.9 \cdot \frac{\text{o}}{\text{min}}$$